1 Paxos Timeline

The timeline consists of two concurrent processes, one on the client Q and one on the client R. In Figure 1 you can see how both clients prepare and propose their values at first, but only the value of client Q gets accepted:

- $T_0 + 0.0$: Q sends a prepare(22,1). As A and B have never accepted a value they reply with acc($\emptyset$,0).
- $T_0 + 0.5$: R sends a prepare(33,2). As B and C have never accepted a value they reply with acc($\emptyset$,0).
- $T_0 + 1.0$: Q sends a propose(22,1). This is acknowledged by A with ack(22,1) because its $n_{max} = 0$. B does not reply as its value $n_{max} = 2$.
- $T_0 + 2.0$: Q sends a prepare(22,3). As B has never accepted a value it replies with acc($\emptyset$,0). A returns the latest accepted value: acc(22,1).
- $T_0 + 2.5$: R sends a propose(33,2). This is acknowledged by C with ack(33,2). B does not reply as its value $n_{max}$ is 3.
- $T_0 + 3.0$: Q sends a propose(22,3). This is acknowledged by A and B with ack(22,3).
- $T_0 + 4.5$: R sends a prepare(33,4). C sends back its latest accepted value acc(33,2). B also sends back its latest accepted value acc(22,3)
- $T_0 + 6.5$: R sends a propose(22,4) (It took the newest value from the prepare phase). Both clients B and C reply with an ack(22,4). All clients have accepted the same value. This means we have achieved consensus.
2 Paxos Acceptors

a) Figure 2 shows an example of how a byzantine client can lead to a failure of the Paxos protocol (i.e. why Paxos is not resilient against byzantine failures):

1. The red proposer sends a prepare with value 1.
2. The red acceptors (incl. the byzantine) send an ack(ø,0) back.
3. The blue proposer sends a prepare with its value.
4. The blue acceptors (incl. the byzantine) send an ack(ø,0) back. We assume that a read on the faulty register of the byzantine node returned $n_{max} = 0$.
5. The red proposer sends a propose with value 1.
6. The red acceptors (incl. the byzantine) send an ack(1,3) back. We assume that a read on the faulty register of the byzantine node returned $n_{max} = 3$.
7. The blue proposer sends a propose with value 1.
8. The blue acceptors (incl. the byzantine) send an ack(2,4) back. We assume that a read on the faulty register of the byzantine node returned $n_{max} = 4$.

At the end of these 8 steps the red proposer thinks that a majority has accepted the value 1 and the blue proposer thinks that a majority has accepted value 2. Both proposers will start to disseminate their value as each of them thinks that they have achieved consensus.

![Diagram](image)

**Figure 2**: How a byzantine client can lead to different values that are accepted by a majority.

b) The prepare step allows the proposer and the acceptor to agree on a lower bound of the proposal number that will be accepted. By sending an ack(x,y) message, the acceptor guarantees the proposer that it will never accept a proposed value that has a smaller timestamp than the one in the prepare message of the proposer.